



Fig. 2. Differences between values of  $C_m/\epsilon$ . Chisholm and McDermott's equations are used as the basis of comparison. The broken line is a fit to values of  $C_m/\epsilon$  derived from the accurate numerical results in [4].

Deviations between numerical data and values obtained with formulas (5) and (6) of [4] are much smaller than those in  $C_g/\epsilon$  and  $C_m/\epsilon$  as reported in the above letter. For example, for  $d/b = 0.4$  (the same utilized here in Figs. 1 and 2) in the range of validity of our interpolating expressions ( $0.12 \leq s/b \leq 3.6$ ) [4], the maximum deviations between numerical and interpolated values of  $Z_{ce}$  and  $Z_{co}$  are

$$0\% \leq \Delta Z_{ce} \leq 1.0\% \\ -0.03\% \leq \Delta Z_{co} \leq 1.4\%.$$

c) In the design of coupled-line filters or directional couplers, some parameters derived from  $Z_{ce}$  and  $Z_{co}$  are of importance, such as

$$Z_m = (Z_{ce} + Z_{co})/2 \\ Z_g = \sqrt{Z_{ce} * Z_{co}} \\ m = (Z_{ce} - Z_{co})/(Z_{ce} + Z_{co}).$$

As far as the accuracy is concerned in evaluating these parameters, it is more convenient to use "ad hoc" expressions (obtained from interpolations of numerical data) than an indirect computation through the expressions for  $Z_{ce}$  and  $Z_{co}$ . A set of such equations, useful for design problems, is reported in [7]. For instance, the parameter  $m$ , which directly governs coupling both in directional couplers and in interdigital and combline filters, can be expressed as

$$m = M(d/b, s/b) * (\ln(\coth(\pi c/2b)))/(\ln(\coth(\pi d/4b)))$$

where  $M(d/b, s/b)$  is a correcting term whose expression is reported in [7]. The above equation guarantees an accuracy with respect to the numerical data of better than 1 percent for  $d/b = 0.4$ .

Finally, we take this opportunity to correct a typing error that occurred in formula (4) of [4]: the exponent of the first term in square brackets should be  $-1/2$ .

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## Corrections to "New Quasi-Static Models for the Computer-Aided Design of Suspended and Inverted Microstrip Lines"

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The following errors appeared in the equations of the above paper<sup>1</sup>:

- a) In equation (3),  $c_i$  should be read as  $C_i$ .
- b) In equation (A2g),  $d^3$  should be replaced by  $f^3$ .
- c) In equation (A3h),  $(486.7425 + 7425 + 279.8 \dots)$  should read  $(486.7425 + 279.8 \dots)$ , i.e., delete 7425.
- d) In equation (A3k),  $-919.36661$  should read  $+919.3661$ .
- e) In equation (A2p),  $161.2689 f^2$  should read  $161.2689 f^3$ .

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<sup>1</sup>R. S. Tomar and P. Bhartia, *IEEE Trans. Microwave Theory Tech.*, vol. MTT-35, pp. 453-457, Apr. 1987.